
VTU QUESTION BANK
Unit 1**Introduction to Finite Automata**

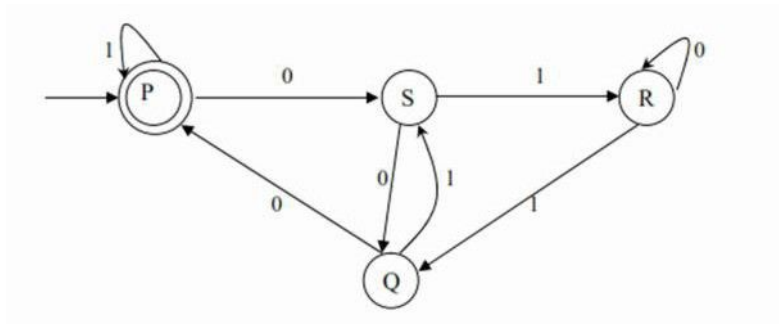
1. Obtain DFAs to accept strings of a's and b's having exactly one a. **(5m) (Dec-2012)**
2. Obtain a DFA to accept strings of a's and b's having even number of a's and b's. **(5m)(Dec-2013)**
3. Give Applications of Finite Automata. **(5m)(Jun-July-2014)**
4. Define DFA, NFA & Language? **(5m)(Dec-2012)**
5. Obtain a DFA to accept strings of a's and b's starting with the string ab. **(6m)(Dec-2013) (Jun-July-2012)**
6. Draw a DFA to accept string of 0's and 1's ending with the string 011. **(4m)(Dec-2013) (Jun-July 2014)**
7. DFA to accept strings of 0's, 1's & 2's beginning with a 0 followed by odd number of 1's and ending with a 2. **(10m)(Dec-2013)(Jun-July-2012)**
8. Design a DFA to accept string of 0's & 1's when interpreted as binary numbers would be multiple of 3 **(5m)(Jun-July-2013, June-July-2014)**
9. Find closure of each state and give the set of all strings of length 3 or less accepted by automaton. **(5m)(Jun-July-2013)**
10. Obtain a DFA to accept strings of a's and b's having a sub string aa. **(5m)(Jun-July-2013)**
11. Write Regular expression for the following $L = \{ a^n b^m : m, n \text{ are even} \}$ $L = \{ a^n, b^m : m \geq 2 \}$, **(5m)(Dec-2012, Jun-July-2014)**
12. Convert above automaton to a NFA to DFA. **(Dec-2013)**

δ		a	b
\square p	{r}	{q}	{p,r}
q	I	{p}	I
*r	{p,q}	{r}	{p}

13. Convert following NFA to DFA using subset construction method. **(10m)(June-July-2014)**

δ_N	0	1
\square p	{p,r}	{q}
q	{r,s}	{p}
*r	{p,s}	{r}
*s	{q,r}	I

14. Convert the following DFA to Regular Expression (10m)(Dec -2012)



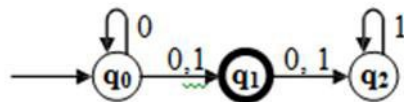
15. Define NFA. With example explain the extended transition function(5m)(Dec-2012)

16. Explain the ground rules of finite automata.(5m)(June-july-2013)

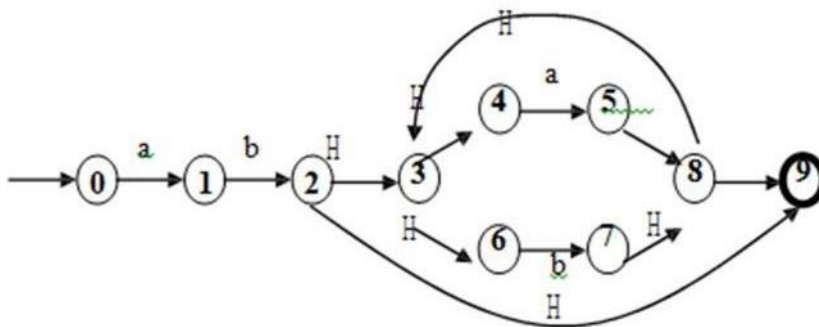
UNIT 2

Finite Automata, Regular Expressions

1. P.T. Let R be a regular expression. Then there exists a finite automaton $M = (Q, \Sigma, G, q_0, A)$ which accepts $L(R)$. **(10m)(June- July2014)**
2. Define derivation , types of derivation , Derivation tree & ambiguous grammar. Give example for each. **(4m)(June- July 2012)**
3. Obtain an NFA to accept the following language $L = \{w \mid w \text{ abab}^n \text{ or } \text{aba}^n \text{ where } n \geq 0\}$ **(6m)(Dec-2013, June- July- 2014)**
4. Convert the following NFA into an equivalent DFA. **(10m))(Dec- Jan 2013) (Jun-July-2012)**



5. Convert the following NFA to its equivalent DFA**(10m))(Dec- Jan 2014) (Jun-July-2012)**

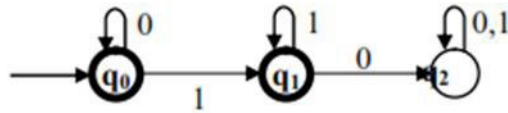


6. Obtain an NFA which accepts strings of a's and b's starting with the string ab. **(7m)(June- July 2013)**
7. Define grammar? Explain Chomsky Hierarchy? Give an example **(6m)(June- July 2014)**
8. Is the following grammar ambiguous **(7m)(Dec-2013, Jun-July-2014)**
 $S \rightarrow aB \mid bA$
 $A \rightarrow aS \mid bAA \mid a$
 $B \rightarrow bS \mid aBB \mid b$

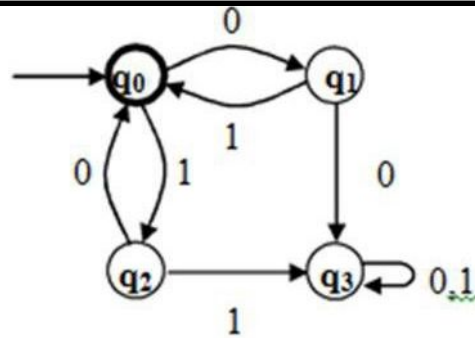
9. Obtain grammar to generate string consisting of any number of a's and b's with at least one b. **(5m)(Dec-2012, June-July-2012)**
10. Obtain a grammar to generate the following language $L = \{WWR \text{ Where } W \in \{a, b\}^*\}$. **(5m)(June-july-2012)**
11. Obtain a grammar to generate the following language: $L = \{ 0^m 1^m 2^n \mid m \geq 1 \text{ and } n \geq 0\}$. **(5m)(Jun-July 2013)**
12. Obtain a grammar to generate the following language: **(5m)(Dec-2013)**
 $L = \{ w \mid n a^{(w)} > n b^{(w)} \}$
 $L = \{ a^n b^m c^k \mid n+2m = k \text{ for } n \geq 0, m \geq 0\}$
13. Define PDA. Obtain PDA to accept the language $L = \{a^n b^n \mid n \geq 1\}$ by a final state. **(5m)(June-july-2012)**
14. Write a short note on application of context free grammar. **(7m)(Dec- 2012)**
15. Explain finite automata with epsilon transition. **(7m)(June-July- 2014)**
16. Explain the application of regular expression **(6m)(June-july- 2012)**

Unit 3
Regular Languages, Properties of Regular Languages

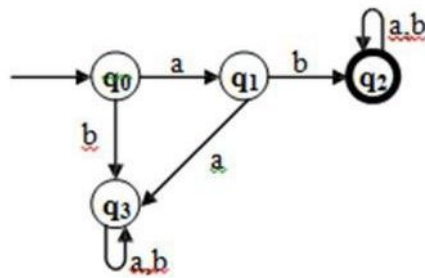
1. Prove pumping lemma? **5m)** (June-July-2012, July-2014)
2. Prove that $L = \{w \mid w \text{ is a palindrome on } \{a,b\}^*\}$ is not regular. i.e., $L = \{aaba, aba, abbbba, \dots\}$ **(8m)**(Dec-2012, June-July 2013)
3. Prove that $L = \{\text{all strings of 1's whose length is prime}\}$ is not regular. i.e., $L = \{1^2, 1^3, 1^5, 1^7, 1^{11}, \dots\}$ **(8m)** (June-July 2013)
4. Let $M = (Q, \Sigma, G, q_0, A)$ be an FA recognizing the language L . Then there exists an equivalent regular expression R for the regular language L such that $L = L(R)$. **(8m)** (Dec- 2013) (Jun-July-2012, Dec-2012)
5. What is the language accepted by the following FA. **(6m)**(Dec 2013 June-July-2013)



6. Write short note on Applications of Regular Expressions **(6m)**(Dec-2013) (Jun-July 2012)
 7. Show that following languages are not regular **(10m)**(June-July 2014)
 - $L = \{a^n b^m \mid n, m \geq 0 \text{ and } n < m\}$
 - $L = \{a^n b^m \mid n, m \geq 0 \text{ and } n > m\}$
 - $L = \{a^n b^m c^m d^n \mid n, m \geq 1\}$
 - $L = \{a^n \mid n \text{ is a perfect square}\}$ $L = \{a^n \mid n \text{ is a perfect cube}\}$
 8. Apply pumping lemma to following languages and understand why we cannot complete proof **(10m)**(June-July 2014 Dec-2012)
 - $L = \{anaba \mid n \geq 0\}$
 - $L = \{anbm \mid n, m \geq 0\}$
 9. Obtain a DFA to accept strings of a's and b's starting with the string ab **(10m)**(Dec-2013)
 10. Obtain a regular expression for the FA shown below: **(10m)** (Dec-Jan 2014 Jun-July-2012)
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11. Solve: (10m)(Dec-Jan12) (Jun-July-2012)



12. Explain Closure properties with an example. (10m)(June-July 2013)

UNIT 4
Context-Free Grammars And Languages

1. P.T. If L and M are regular languages, then so is $L \cap M$. **(10m)(June-July 2012)**
2. Write a DFA to accept the intersection of $L_1=(a+b)^*a$ and $L_2=(a+b)^*b$ that is for $L_1 \cap L_2$. **(10m)(June-July 2012, Jun-July-2013)**
3. Find the DFA to accept the intersection of $L_1=(a+b)^*ab (a+b)^*$ and $L_2=(a+b)^*ba (a+b)^*$ and that is for $L_1 \cap L_2$ **(10m)(Dec-2013, Jun-July-2014)**
4. P.T. If L and M are regular languages, then so is $L - M$. **(10m)(Dec-2012)**
5. Design context-free grammar for the following cases**(10m)(Dec-2013, June-July 2014)**
 $L=\{ 0^n 1^n \mid n$
 $L=\{a^i b^j c^k \mid i \neq j \text{ or } j \neq k\}$
6. Generate grammar for RE $0^*1(0+1)^*$ **(10m)(June-July 2014)**
7. P.T. If L is a regular language over alphabet S, then $L = \Sigma^* \cdot L$ is also a regular language. **(8m) (Dec-Jan 2014) (Jun-July-2012)**
8. P.T. - If L is a regular language over alphabet Σ , then, $L = \Sigma^* \cdot L$ is also a regular language. **(8m) (Dec 2012, Dec-2013)**
9. P.T. If L is a regular language, so is L^R **(6m)(Dec-2012) (Jun-July-2014)**
10. . If L is a regular language over alphabet Σ , and h is a homomorphism on Σ , then $h(L)$ is also regular. **(10m)(June-july- 2012).**
11. Explain CGF with an example. . **(5m)(Jun-July-2014)**
12. Explain decision properties of regular language. . **(5m)(Jun-July-2013)**

UNIT 5

Pushdown Automata

1. Give leftmost and rightmost derivations of the following strings
 a. 00101 b) 1001 c) 00011 **(4m) (June-July 2012) (Dec-2013)**
2. Construct PDA: For the language **(4m)(June-July2014)**

$$L = \{wcw^R \mid w \in \{a, b\}^*, c \in \Sigma\}$$

3. Construct DPDA which accepts the language $L = \{wcw^R \mid w \in \{a, b\}^*, c \in \Sigma\}$.
(4m)(June-July 2013)
4. Construct DPDA for the following: Accepting the language of balanced parentheses. (Consider any type of parentheses) Accepting strings with number of a's is more than number of b's Accepting $\{0^n 1^m \mid n \neq m\}$ **(8M)(June-July-2012)**
5. Design nPDA to accept the language: **(10m) (Dec-2013)**
 $\{a^i b^j c^k \mid i, j, k \geq 0 \text{ and } i = j \text{ or } i = k\}$
 $\{a^i b^j c^{i+j} \mid i, j \geq 0\}$
 $\{a^i b^{i+j} c^j \mid i \geq 0, j \geq 1\}$
6. Construct PDA: For the language $L = \{a^n b^{2n} \mid a, b \in \Sigma, n \geq 0\}$ **(5m) (Dec-2012, July-2013)**
7. Construct PDA to accept if-else of a C program and convert it to CFG. (This does not accept if-else-else statements) **(5m)(Dec-2013)**
8. Show that deviation for the string aab is ambiguous. **(5m)(June 2014)**
9. Suppose h is the homomorphism from the alphabet $\{0,1,2\}$ to the alphabet $\{a,b\}$ defined by $h(0) = a$; $h(1) = ab$ & $h(2) = ba$
 a) What is $h(0120)$?
 b) What is $h(21120)$?
 c) If L is the language $L(01^*2)$, what is $h(L)$?
 d) If L is the language $L(0+12)$, what is $h(L)$?
 If L is the language $L(a(ba)^*)$, what is $h^{-1}(L)$? **(5m) (Dec-2013)**
10. Design a PDA to accept the set of all strings of 0's and 1's such that no prefix has more 1's than 0's. **(5m)(June 2012)**
11. Construct PDA: Accepting the set of all strings over $\{a, b\}$ with equal number of a's and b's. Show the moves for abbaba. **(5m) (June 2013)**
12. Construct PDA: Accepting the language of balanced parentheses, (consider any type of parentheses). **(5m)(Dec-2012)**

13. How do you convert From PDA to CFG. (5m)(Dec-2013)

14. Convert PDA to CFG. PDA is given by $P = (\{p,q\}, \{0,1\}, \{X,Z\}, \delta, q, Z)$,
Transition function δ is defined by (5m)(Dec-2012)

$$\delta(q, 1, Z) = \{(q, XZ)\}$$

$$\delta(q, 1, X) = \{(q, XX)\}$$

$$\delta(q, H, X) = \{(q, H)\}$$

$$\delta(q, 0, X) = \{(p, X)\}$$

$$\delta(p, 1, X) = \{(p, H)\}$$

15. Convert to PDA, CFG with productions (10m)(Dec-2012)

$$A \rightarrow aAA, A \rightarrow aS \mid bS \mid a$$

$$S \rightarrow SS \mid (S) \mid H$$

$$S \rightarrow aAS \mid bAB \mid aB,$$

$$A \rightarrow bBB \mid aS \mid a,$$

$$B \rightarrow bA \mid a$$

16. Explain push down automata with an example(10m)(Dec- 2013)

UNIT 6
Properties of Context-Free Languages

1. Eliminate the non-generating symbols from $S \rightarrow aS \mid A \mid C, A \rightarrow a, B \rightarrow aa, C \rightarrow aCb$. **(8m)(June 2012)**
2. Draw the dependency graph as given above. A is non-reachable from S. After eliminating A, $G = (\{S\}, \{a\}, \{S \rightarrow a\}, S)$. **(6m)(June 2013)**
3. Find out the grammar without H – Productions $G = (\{S, A, B, D\}, \{a\}, \{S \rightarrow aS \mid AB, A \rightarrow H, B \rightarrow H, D \rightarrow b\}, S)$. **(6m)(June 2014)**
4. Eliminate non-reachable symbols from $G = (\{S, A\}, \{a\}, \{S \rightarrow a, A \rightarrow a\}, S)$ **(10m)(Dec-2013)**
5. Eliminate non-reachable symbols from $S \rightarrow aS \mid A, A \rightarrow a, B \rightarrow aa$. **(10m)(Dec-2012)**
6. Eliminate useless symbols from the grammar with productions $S \rightarrow AB \mid CA, B \rightarrow BC \mid AB, A \rightarrow a, C \rightarrow AB \mid b$. **(5m)(June 2014)**
7. Eliminate useless symbols from the grammar **(5m)(June 2012)**
 $P = \{S \rightarrow aAa, A \rightarrow Sb \mid bCC, C \rightarrow abb, E \rightarrow aC\}$
 $P = \{S \rightarrow aBa \mid BC, A \rightarrow aC \mid BCC, C \rightarrow a, B \rightarrow bcc, D \rightarrow E, E \rightarrow d\}$
 $P = \{S \rightarrow aAa, A \rightarrow bBB, B \rightarrow ab, C \rightarrow aB\}$
 $P = \{S \rightarrow aS \mid AB, A \rightarrow bA, B \rightarrow AA\}$.
8. Write Algorithm to find nullable variables. **(5m)(June 2012)**
9. Eliminate H - productions from the grammar. **(5m)(Dec-2012, Dec-2013)**
 $S \rightarrow a \mid Xb \mid aYa, X \rightarrow Y \mid H, Y \rightarrow b \mid X$
 $S \rightarrow Xa, X \rightarrow aX \mid bX \mid H$
 $S \rightarrow XY, X \rightarrow Zb, Y \rightarrow bW, Z \rightarrow AB, W \rightarrow Z, A \rightarrow aA \mid bB \mid H, B \rightarrow Ba \mid Bb \mid H$
 $S \rightarrow ASB \mid H, A \rightarrow aAS \mid a, B \rightarrow SbS \mid A \mid bb$
10. Eliminate H - productions and useless symbols from the grammar $S \rightarrow a \mid aA \mid B \mid C, A \rightarrow aB \mid H, B \rightarrow aA, C \rightarrow aCD, D \rightarrow dd$. **(10m)(Dec-2012)**
11. Show that $L = \{a^i b^j c^k \mid i \neq j\}$ is not CFL. **(10m)(Dec-2013)**
12. Show that $L = \{ww \mid w \in \{0, 1\}^*\}$ is not CFL. **(10m)(June 2014)**
13. Using pumping lemma for CFL prove that below languages are not context free $\{p \mid p \text{ is a prime}\}$. **(10m)(Dec-2013)**

UNIT 7

Introduction To Turing Machine

1. Explain with example problems that Computers cannot solve. **(6m)(June-2012)**
2. Explain briefly the following Halting problem. **(4m)(June 2013)**
3. Explain Programming techniques for Turning Machines. **(10m)(Dec-Jan-2010)**
4. Design a Turing machine to accept a Palindrome. **(10m)(Dec-2013)**
5. Design a TM to recognize a string of the form $a^n b^{2n}$. **(10m)(Dec-2013)**
7. Define undesirability, decidability. **(10m)(June 2014)**
8. Post's Correspondence problem Design a TM to recognize a string of 0s and 1s such that the number of 0s is not twice as that of 1s. **(10m) (June- 2012, Dec-2013)**

UNIT 8

Undecidability

1. Design a TM to recognize a string of the form $a^n b^{2n}$. **(10m) (June- 2013)**
2. P.t If L is a recursive language, L is also recursive. **(10m) (June 2014)**
3. Design a Turing Machine to recognize $0^n 1^n 2^n$. **(10m)(Dec-2013)**
4. Explain briefly the following Halting problem **(6m)(Dec-2012, Dec-2013)**
5. Post's Correspondence problem Design a TM to recognize a string of 0s and 1s such that the number of 0s is not twice as that of 1s **(10m)(Dec-2012)**
7. Design a Turing machine to accept a Palindrome. **(7m)(Dec-2013)**
8. Write a short note on: **(20m) Dec-2012)**
 - a. Undesirability
 - b. Halting problem
 - c. decidability.