KENDRIYA VIDYALAYA GACHIBOWLI, GPRA CAMPUS, HYD-32 SAMPLE PAPER 02 FOR SESSION ENDING EXAM (2018-19)

SUBJECT: MATHEMATICS(041)

BLUE PRINT : CLASS XI

| Unit | Chapter | VSA (1 mark) | SA (2 marks) | LA – I (4 marks) | LA– II (6 marks) | Total |
|-------------------------------|---|-----------------|-----------------|---------------------|---------------------|---------|
| Sets & functions | Sets | 1(1) | | 4(1) | 6(1) | 11(3) |
| | Relations and Functions | | 2(1)* | 4(1) | | 06(2) |
| | Trigonometric Functions | | 2(1) | 4(1)* | 6(1)* | 12(3) |
| Algebra | Principle of Mathematical Induction | | | | 6(1)* | 6(1) |
| | Complex Numbers and Quadratic Equations | | 2(1) | 4(1) | | 6(2) |
| | Linear Inequalities | | | 4(1) | | 4(1) |
| | Permutations and Combinations | 1(1)* | | | 6(1) | 7(2) |
| | Binomial Theorem | | 2(1)* | 4(1)* | | 6(2) |
| | Sequences and Series | | 2(1)* | | 6(1)* | 8(2) |
| Coordinate geometry | Straight Lines | 1(1) | | 4(1)* | | 5(2) |
| | Conic Sections | | | 4(1) | | 4(1) |
| | Introduction to Three Dimensional Geometry | | | 4(1) | | 4(1) |
| Calculus | Limits and Derivatives | | 2(1) | 4(1) | | 6(2) |
| Mathematical reasoning | Mathematical Reasoning | 1(1) | 2(1) | | | 3(2) |
| Statistics & probability | Statistics | | | | 6(1) | 6(1) |
| | Probability | | 2(1) | 4(1) | | 6(2) |
| | Total | 4(4) | 16(8) | 44(11) | 36(6) | 100(29) |

Note: * - Internal Choice Questions

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General Instruction:

(i) All questions are compulsory.

(ii) This question paper contains 29 questions.

(iii) Question 1- 4 in Section A are very short-answer type questions carrying 1 mark each.

(iv) Question 5-12 in Section B are short-answer type questions carrying 2 marks each.

(v) Ouestion 13-23 in Section C are long-answer-I type questions carrying 4 marks each.

(vi) Question 24-29 in Section D are long-answer-II type questions carrying 6 marks each.

<u>SECTION – A</u> Questions 1 to 4 carry 1 mark each.

- 1. Let $A = \{1, 2, 3, 4, 5, 6\}, B = \{2, 4, 6, 8\}$. Find A B and B A.
- **2.** If ${}^{16}C_r = {}^{16}C_{r+2}$, then find ${}^{r}C_4$

OR

Find n, if : Find the L.C.M. of 6!, 8!, 9!, 11!.

- **3.** Line through the points (- 2, 6) and (4, 8) is perpendicular to the line through the points (8, 12) and (x, 24). Find the value of x.
- 4. Write converse of, if two lines are parallel, then they do not intersect in same plane.

<u>SECTION – B</u> Questions 5 to 12 carry 2 marks each.

- 5. Let A = {1, 2, 3, 5} and B = {4, 6, 9}. Define a relation R from A to B by R = {(x, y) : x y is odd natural number, $x \in A$, $y \in B$. Write R in roster form.
- 6. Solve the equation: $\sqrt{5}x^2 + x + 5 = 0$.
- 7. Find the coefficient of x^6y^3 in the expansion of $(x + 2y)^9$.

OR

Find a positive value of m for which the coefficient of x^2 in the expansion $(1 + x)^m$ is 6.

- 8. One card is drawn from a well shuffled deck of 52 cards. If each outcome is equally likely, calculate the probability that the card will be (i) a diamond (ii) not an ace
- 9. Write the component statements of the following compound statements and check whether the compound statement is true or false: "A line is straight and extends indefinitely in both directions."
- 10. Let A = {1, 2, 3, 4, 6}. Let R be the relation on A defined by {(a, b): $a, b \in A, b$ is exactly divisible by a. (i) Find the domain of R (ii) Find the range of R.

OR

Let $f = \{(1, 1), (2, 3), (0, -1), (-1, -3)\}$ be a function from Z to Z defined by f(x) = ax + b, for some integers a and b. Determine a, b.

MAX. MARKS : 100 DURATION: 3 HRS 11. In any triangle ABC, prove that $\frac{\sin(A-B)}{\sin(A+B)} = \frac{(a^2 - b^2)}{c^2}$

12. If a, b, c are in A.P., prove that the following is also in A.P. : b + c - a, c + a - b, a + b - cOR

Insert 3 arithmetic means between 2 and 10.

<u>SECTION – C</u> Questions 13 to 23 carry 4 marks each.

13. Find the domain and range of the function $f(x) = \sqrt{9 - x^2}$

- **14.** Show that for any sets A and B, $A = (A \cap B) \cup (A B)$ and $A \cup (B A) = (A \cup B)$
- **15.** A committee of 7 has to be formed from 9 boys and 4 girls. In how many ways can this be done when the committee consists of: (i) exactly 3 girls ? (ii) at least 3 girls ? (iii) at most 3 girls ?
- 16. Find the distance of the line 4x y = 0 from the point P (4, 1) measured along the line making an angle of 135° with the positive *x*-axis.

OR

In the triangle ABC with vertices A (2, 3), B (4, -1) and C (1, 2), find the equation and length of altitude from the vertex A.

17. The second, third and fourth terms in the binomial expansion $(x + a)^n$ are 240, 720 and 1080, respectively. Find x, a and n.

OR

The coefficients of three consecutive terms in the expansion of $(1 + a)^n$ are in the ratio 1: 7 : 42. Find *n*.

18. Find the modulus and argument of the complex number $\frac{1+i}{1-i} - \frac{1-i}{1+i}$.

- **19.** Find the derivative of sin (5x 8) with respect to first principle.
- **20.** A point R with *x*-coordinate 4 lies on the line segment joining the points P(2, -3, 4) and Q (8, 0, 10). Find the coordinates of the point R.
- **21.** A man running a racecourse notes that the sum of the distances from the two flag posts from him is always 10 m and the distance between the flag posts is 8 m. Find the equation of the posts traced by the man.
- **22.** In a relay race there are five teams A, B, C, D and E. (a) What is the probability that A, B and C finish first, second and third, respectively. (b) What is the probability that A, B and C are first three to finish (in any order) (Assume that all finishing orders are equally likely)

23. Prove that: $\frac{\sin 7x + \sin 5x + \sin 9x + \sin 3x}{\cos 7x + \cos 5x + \cos 9x + \cos 3x} = \tan 6x$ OR Solve : secx - tanx = $\sqrt{3}$

<u>SECTION – D</u> Questions 24 to 29 carry 6 marks each.

24. Prove by Principle of Mathematical Induction $\forall n \in N$:

$$1.2.3 + 2.3.4 + 3.4.5 + \dots + n(n+1)(n+2) = \frac{n(n+1)(n+2)(n+3)}{4}$$

Prove that $\frac{1}{3.5} + \frac{1}{5.7} + \frac{1}{7.9} + \dots + \frac{1}{(2n-1)(2n+1)} = \frac{n}{3(2n+3)}$ by principle of Mathematical induction for $\forall n \in N$

25. Find the sum of the following series up to *n* terms: $\frac{1^3}{1} + \frac{1^3 + 2^3}{1 + 3} + \frac{1^3 + 2^3 + 3^3}{1 + 3 + 5} + \dots$

Let S be the sum, P the product and R the sum of reciprocals of *n* terms in a G.P. Prove that $P^2R^n = S^n$.

- 26. If $\tan x = \frac{3}{4}, \pi < x < \frac{3\pi}{2}$ then find the value of $\sin \frac{x}{2}, \cos \frac{x}{2}$ and $\tan \frac{x}{2}$. OR In any triangle ABC, prove that $(b^2 - c^2)\cot A + (c^2 - a^2)\cot B + (a^2 - b^2)\cot C = 0$.
- **27.** A well known thinking about the students of senior secondary school is that they are brilliant, unique in maths. A maths teacher taught them properly and then he decided to take a test to justify them. He prepared a test consists 12 questions divided in two parts say part I and part II, containing 5 and 7 questions respectively. A student is required to attempt 8 questions in all, selecting atleast 3 from each part. In how many ways can a student select the questions ?
- **28.** A college warded 38 medals in football, 15 in basketball and 20 in cricket. If these medals went to a total of 58 men and only three men got medals in all the three sports, how many received medals in exactly two of the three sports ? How many received exactly one medal of the three sports?
- **29.** The mean of 5 observations is 4.4 and their variance is 8.24. If three of the observations are 1, 2 and 6, find the other two observations.

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