MAHATMA GANDHI UNIVERSITY PG-CSS MODEL QUESTION PAPER 2012 SEMESTER I

PAPER: PH1RC2 CLASSICAL MECHANICS AND RELATIVITY

Time : 3 hrs

Total Weight:30

Part A (Short answer questions)

(Answer any six questions. Each question carries weight one.)

- 1. What are the generalised coordinates? What are the advantages of using them?
- 2. What are Poisson Brackets?
- 3. What are action and angle variables?
- 4. What is the importance of Perturbation theory in classical mechanics
- 5. Distinguish between Time-independent and Time-dependent perturbations
- 6. Show that rigid body has six degrees of freedom
- 7. Explain coriolis force
- 8. What are Euler angle.
- 9. Write notes on relativistic Doppler effect.
- 10. Briefly explain the principle of covariance.

Part B (Problems)

(Answer any four questions. Each question carries weight two.)

11. Show that the transformation of $Q = \log {\binom{\sin p}{q}}$ and $P = q \cot p$ is canonical and find the concerting function

find the generating function

- 12. Using Lagrange's equation derive an expression for the period of oscillation of a linear harmonic oscillator.
- 13. Apply time dependent perturbation theory to the case of a simple pendulum with finite amplitude
- 14. Show that the moment of inertia is a symmetric second rank tensor.
- 15. Show that the angular acceleration is the same in fixed and rotating frames of reference.
- 16. How fast and in what direction must galaxy A be moving if an absorption line found at wavelength 550nm (green) for a stationary galaxy is shifted to 450 nm (blue) (a "blue-shift") for galaxy A?

4x2=8 weight

t

Part C (Essay)

(Answer all questions. Each question carries weight four.)

17. Using the Hamilton's principle of least action derive the Lagrange's equations for system of particles OR

Obtain Lagrange's equations for a simple pendulum

18. (i)Derive the equation of motion for all angles for a heavy symmetrical top with one point fixed. Discuss the precession and nutation qualitatively OR

(ii) What are normal vibrations and normal co-ordinates? Discuss the small oscillations of the CO_2 molecule and obtain the frequencies of their modes.

19. (i) Obtain Hamiltonian formulation for continuous systems OR

(ii) Outline Lagrangian formulation of a continuous system and discuss sound vibrations in a gas

20. (i) Deduce Lagrangian and Hamilltonian of a relativistic particle, OR

(ii) Obtain Schwarzchild's exterior solution for the gravitational field of a single mass at rest and explain on the basis of this solution the advance of the perihelion of the planet Mercury.

4x4 = 16 weight