

RAMAKRISHNA MISSION VIDYAMANDIRA

Belur Math, Howrah – 711 202

ADMISSION TEST – 2017 MATHEMATICS (Honours)

Date : 14-06-2017

Full Marks : 50

Time: 11·00 a.m. – 12·00 noon

Instructions for the candidate

Answer all the questions given below. Each question carries **2 marks** for correct answer and **-1 mark** for wrong answer. Tick (✓) the correct option. The tick must be very clear — if it is smudgy or not clear, no marks will be awarded. **Calculator is not allowed.**

Name of the student : _____

Application No. : _____

Signature of the invigilator : _____

- Equation of the ellipse with x and y axes as its major and minor axes respectively, passing through the point (-3, 1) and with eccentricity $\sqrt{\frac{2}{5}}$ is
a) $3x^2 + 5y^2 = 32$, b) $6x^2 + 10y^2 = 32$, c) $5x^2 + 3y^2 = 32$, d) none of these.
- The locus of the point of intersection of the straight lines $\frac{tx}{a} + \frac{y}{b} - t = 0$ & $\frac{x}{a} - \frac{ty}{b} + 1 = 0$ is
a) a circle, b) a parabola, c) an ellipse, d) none of these.
- If one of the diameters of the circle A with equation $x^2 + y^2 - 2x - 6y + 6 = 0$ is a chord to the circle B with centre (2, 1) then the radius of the circle B is
a) $\sqrt{3}$, b) $\sqrt{2}$, c) 3, d) 2.
- 99th term of the series $2 + 7 + 14 + 23 + 34 + \dots$ is
a) 9999, b) 9998, c) 10000, d) none of these.
- The sum of all natural numbers between 0 and 100 which are not divisible by 5 is
a) 4000, b) 4050, c) 1050, d) 4005.
- If $\vec{a}, \vec{b}, \vec{c}, \vec{d}$ are unit vectors such that $(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 1$ and $\vec{a} \cdot \vec{c} = \frac{1}{2}$ then
a) $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar, b) $\vec{b}, \vec{c}, \vec{d}$ are non-coplanar,
c) \vec{b}, \vec{d} are non-parallel, d) \vec{a}, \vec{d} are parallel and \vec{b}, \vec{c} are parallel.
- If $I = \int_{-1}^2 |x \sin \pi x| dx$ then I equals
a) $\frac{1}{\pi}$, b) $\frac{2}{\pi}$, c) $\frac{4}{\pi}$, d) $\frac{5}{\pi}$.

8. Let f be a non-negative function defined on the interval $[0,1]$. If $\int_0^x \sqrt{1 - \{f'(t)\}^2} dt = \int_0^x f(t) dt$, $0 \leq x \leq 1$ and $f(0) = 0$ then
- a) $f\left(\frac{1}{2}\right) < \frac{1}{2}$ and $f\left(\frac{1}{3}\right) > \frac{1}{3}$, b) $f\left(\frac{1}{2}\right) > \frac{1}{2}$ and $f\left(\frac{1}{3}\right) > \frac{1}{3}$,
- c) $f\left(\frac{1}{2}\right) < \frac{1}{2}$ and $f\left(\frac{1}{3}\right) < \frac{1}{3}$, d) $f\left(\frac{1}{2}\right) > \frac{1}{2}$ and $f\left(\frac{1}{3}\right) < \frac{1}{3}$.
9. If $I = \int_{\frac{1}{e}}^e |\log x| \frac{dx}{x^2}$, then I equals
- a) $2\left(1 - \frac{1}{e}\right)$, b) 2, c) $\frac{2}{e}$, d) 0.
10. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined by $f(x) = 2x + \sin x$ for $x \in \mathbb{R}$. Then f is
- a) one-one and onto, b) one-one but not onto,
c) onto but not one-one, d) neither one-one nor onto.
11. For the circle $x^2 + y^2 = r^2$, the value of r for which the area enclosed by the tangents drawn from the point $(6,8)$ to the circle and the chord of contact is maximum is
- a) 10, b) 5, c) $5\sqrt{2}$, d) none of these.
12. Which of the following function is differentiable at $x = 0$?
- a) $\cos(|x|) + |x|$, b) $\cos(|x|) - |x|$, c) $\sin(|x|) + |x|$, d) $\sin(|x|) - |x|$.
13. Let $\mathbb{Q}, \mathbb{R}, \mathbb{R} - \mathbb{Q}$ denote respectively the set of all rational numbers, real numbers and irrational numbers. Suppose $p \in \mathbb{R} - \mathbb{Q}$ and $\mathbb{Q} + p = \{x + p : x \in \mathbb{Q}\}$. Then
- a) $\mathbb{Q} \cup (\mathbb{Q} + p) = \mathbb{R}$, b) $\mathbb{Q} + p = \mathbb{R} - \mathbb{Q}$ if p is transcendental,
c) $\mathbb{Q} + p = \mathbb{R} - \mathbb{Q}$ if p is algebraic, d) $\mathbb{Q} + p$ is a proper subset of $\mathbb{R} - \mathbb{Q}$.
14. Let $|X| = 4$, $|Y| = 3$. The number of surjective maps from X to Y is
- a) 24, b) 30, c) 36, d) none of these.
15. Let the relation ρ be defined on \mathbb{Z} (the set of all integers) by ' $a \rho b$ iff $ab \geq 0$; $a, b \in \mathbb{Z}$ '. Then ρ is
- a) Reflexive but neither symmetric nor transitive, b) Reflexive and symmetric but not transitive,
c) Reflexive and transitive but not symmetric, d) An equivalence relation.
16. Let A be any 2×2 matrix and B be its adjoint. Then the determinant of the product matrix AB is
- a) 1, b) $\det A$, c) $(\det A)^2$, d) none of these.

17. Let A and B be two matrices of order 2×2 . If they have a common row and same determinant, then which one of the following statements is true?

- a) $A = B$,
 b) adjoint of A = adjoint of B,
 c) $\det(AB) = (\det(A))^2$,
 d) $\det(A+B) = \det A + \det B$.

18. The smallest number whose square exceeds the number by 2 is

- a) 1, b) 2, c) -1, d) -2.

19. The sum of two prime numbers is 61. The sum of their squares is

- a) 2195, b) 2875, c) 3485, d) none of these.

20. The determinant of the matrix $A = \begin{bmatrix} x^2 + x & x^3 + x^2 & x^4 + x^3 \\ x^2 & x^3 & x^4 \\ x^2 - x & x^3 - x^2 & x^4 - x^3 \end{bmatrix}$, $x \in \mathbb{R}$ is

- a) a polynomial in x of degree 7, b) 0,
 c) a polynomial in x of degree 9, d) none of these.

21. If E_1 and E_2 are the events associated to a random experiment and if E_1 implies E_2 , then

- a) $P(E_1) < P(E_2)$, b) $P(E_1) \leq P(E_2)$, c) $P(E_1) \geq P(E_2)$, d) $P(E_1) > P(E_2)$.

22. The probability of drawing a card which is either a spade or a king from a well-shuffled pack of cards is

- a) $\frac{1}{26}$, b) $\frac{17}{52}$, c) $\frac{1}{52}$, d) $\frac{4}{13}$.

23. The area of the region bounded by the curves $y = x^2$ and $x = y^2$ is

- a) $\frac{1}{2}$, b) $\frac{1}{3}$, c) $\frac{1}{4}$, d) none of these.

24. The curves $x^2 - y^2 = 8$, $xy = 3$ intersect at an angle

- a) $\frac{\pi}{3}$, b) $\frac{\pi}{2}$, c) $\frac{\pi}{4}$, d) none of these.

25. The maximum value of $\left(\frac{1}{x}\right)^x$ is

- a) $\left(\frac{1}{e}\right)^e$, b) e^e , c) $e^{\frac{1}{e}}$, d) none of these.

_____ × _____