

24. Let $\gamma(t) = e^{it}$, $0 \leq t \leq 2\pi$

1) $\int_{\gamma} \sin\left(\frac{1}{z}\right) dz = 0$

2) $\int_{\gamma} \sin^2\left(\frac{1}{z}\right) dz = 1$

3) $\int_{\gamma} \sin\frac{1}{z} dz = 2\pi i$

4) $\int_{\gamma} \sin^2\left(\frac{1}{z}\right) dz = 2\pi i$

25. If f is an entire function such that $f(z) \rightarrow \infty$ as $z \rightarrow \infty$ then

- 1) f has a residue at $z = 0$
- 2) f has a simple pole at $z = \infty$
- 3) f has an essential singularity at $z = \infty$
- 4) f has a pole at $z = \infty$ but need not be simple

26. Let G be a group of order 231. The number of elements of order 11 in G is _____.

- 1) 10
- 2) 12
- 3) 11
- 4) 2

27. A sylow 3-subgroup of a group of order 12 has order

- 1) 3
- 2) 4
- 3) 12
- 4) 8

28. The number of homomorphism from z_{10^5} to z_{100} are

- 1) 100
- 2) 200
- 3) 30
- 4) 40

29. How many positive integers not exceeding 1000 are divisible by 7 or 11?

- 1) 142
- 2) 90
- 3) 220
- 4) 12

30. The remainder when 9^{10} is divided by 11 is

- 1) 1
- 2) 2
- 3) 5
- 4) 0

31. The primitive root mod 18 is _____.

- 1) 3
- 2) 5
- 3) 6
- 4) 9

32. Let $X = \{1, 2, 3, 4, 5\}$ and $\tau = \{X, \Phi, \{2\}, \{3, 4\}, \{2, 3, 4\}, \{1, 3, 4\}, \{1, 2, 3, 4\}\}$ then the τ -exterior of $\{3\}$ is

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| 1) $\{2\}$ | 2) $\{2, 3\}$ |
| 3) $\{2, 4\}$ | 4) Φ |

33. A discrete space X is separable iff X is

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| 1) Uncountable | 2) Countable |
| 3) Finite | 4) Infinite |

34. Let τ be the topology on N which consist of Φ and all subsets of N of the form $E_n = \{n, n+1, n+2, \dots\}$ where $n \in N$, then the accumulation points of set A is

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| 1) $A' = \{1, 2, 3, \dots, 34, 35, 36\}$ | 2) $A' = \{1\}$ |
| 3) Φ | 4) N |

35. Consider the topology $\tau = \{X, \Phi, \{x\}, \{z, w\}, \{x, z, w\}, \{y, z, w, u\}\}$ on $X = \{x, y, z, w, u\}$ then the number of components of X is

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| 1) 1 | 2) 2 |
| 3) 3 | 4) 4 |

36. Let $f : X \rightarrow Y$ and $g : X \rightarrow Y$ be continuous functions from a topological space X into a Hausdorff space Y . Then $A = \{x : f(x) = g(x)\}$ is

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| 1) closed subset of X | 2) open subset of X |
| 3) not a closed subset of X | 4) not a open subset of X |

37. Every projection $\pi_i : X \rightarrow X_i$ on a product space $X = \prod_i X_i$ is

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| 1) Only continuous | 2) Bi-continuous |
| 3) Only open | 4) Neither continuous nor open |

38. The projection map $\Pi_1 : X \times Y \rightarrow X$ is a closed map if

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| 1) X is compact | 2) Y is compact |
| 3) X is connected | 4) Y is connected |

39. Bernoulli's differential equation is given by _____.

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| 1) $\frac{dy}{dx} + P(x)y = Q(x)y^n$ | 2) $\frac{dy}{dx} + y = Q(x)y^2 + R(x)$ |
| 3) $\frac{dy}{dx} + P(x)y = Q(x)y^2$ | 4) $\frac{dy}{dx} + P(x)y = Q(x)$ |

52. The solution of the integral equation $S = \int_0^s \frac{g(t)}{(s-t)^{1/2}} dt$ is

1) $g(t) = \frac{2t^{1/2}}{\pi}$

2) $g(t) = \frac{3t^{1/2}}{\pi}$

3) $g(t) = \frac{t^2}{\pi}$

4) $g(t) = -\frac{t^2}{\pi}$

53. The resolvent kernel of integral equation $\phi(x) = \sin x + 2 \int_0^x e^{x-t} \phi(t) dt$ is

1) $e^{2(x-t)}$

2) $e^{3(x-t)}$

3) $e^{(x-t)}$

4) $e^{(x+t)}$

54. Given the homogeneous integral equation $\phi(x) = \lambda \int_1^2 \left(x\xi + \frac{1}{x\xi} \right) \phi(\xi) d\xi$

1) Not a Fredholm integral equation

2) The eigen function of the system is $\lambda^2 + 13\lambda + 6 = 0$

3) The required eigen values are $\lambda_1 = \frac{1}{2}[17 + \sqrt{265}] = 6.639$ and

$$\lambda_2 = \frac{1}{2}[17 - \sqrt{265}] = 0.3606$$

4) The eigen values are 0.037 and 3.3259

55. The principal moment of inertia for a homogeneous sphere of radius R and mass M is

1) $\frac{3}{5}MR^2$

2) $\frac{1}{2}MR^2$

3) $\frac{2}{5}MR^2$

4) $\frac{3}{2}MR^2$

56. A frame of reference in which law of inertia holds

1) Non-Newtonian frame of reference

2) Accelerated frame of reference

3) Newtonian frame of reference

4) Galilean frame of reference

57. The point of support of a simple pendulum moves on an ellipse fixed in the same plane with the parametric equation $x = a \cos \omega t$, $y = a \sin \omega t$, $\omega = \text{constant}$. The Lagrange equation of motion of the bob for small oscillations is $\ddot{\theta} + \frac{g\theta}{l} F(t) = \frac{aw^2}{l} \cos \omega t$. Then the value of the function $F(t)$ is

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| 1) $1 + \frac{bw^2}{g} \sin \omega t$ | 2) $1 - \frac{bw^2}{g} \cos \omega t$ |
| 3) $\frac{bw^2}{g} \cos \omega t$ | 4) $\frac{bw^2}{g} \sin \omega t$ |

58. In any system of particles, suppose we do not assume that the internal force come in pairs. Then the fact that the sum of internal force is zero follows from

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|---------------------------|-------------------------------------|
| 1) Newton's Second law | 2) Conservation of angular momentum |
| 3) Conservation of energy | 4) Principle of virtual energy |

59. In spherical pendulum, a small bob of mass m is constrained to move on a smooth spherical surface, of radius R , R being the length of the pendulum, the equation of motion is

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| 1) $mgR \cos^2 \theta = 0$ | 2) $\ddot{\theta} - mR^2 \cos^2 \theta \dot{\phi}^2 = 0$ |
| 3) $mR^2 \sin^2 \theta \dot{\phi}^2 = \text{constant}$ | 4) $mR^2 \cos^2 \theta \dot{\phi}^2 = \text{constant}$ |

60. A continuous random variable X has the density function $f(x) = \frac{c}{1+x^2}$, $-\infty < x < \infty$ then the value of c is

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|---------------------|---------------------|
| 1) $-\frac{1}{\pi}$ | 2) $\frac{2}{\pi}$ |
| 3) $\frac{1}{\pi}$ | 4) $-\frac{2}{\pi}$ |

61. Out of 800 families with 4 children each, how many families would be expected to have 2 boys and 2 girls. Assume equal probabilities for boys and girls

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| 1) 750 | 2) 550 |
| 3) 300 | 4) 700 |

62. A problem in statistics is given to three students A , B and C whose chances of solving it are $\frac{1}{2}$, $\frac{3}{4}$ and $\frac{1}{4}$ respectively. What is the probability that the problem will be solved if all of them try independently?

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| 1) $\frac{1}{2}$ | 2) $\frac{29}{32}$ |
| 3) $\frac{3}{4}$ | 4) $\frac{1}{4}$ |

ROUGH WORK

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