

**Indian Statistical Institute**  
**Junior Research Fellowship in Geology, Entrance Examination**  
**2015**

TEST CODE: **GEA**

BOOKLET No.

**Forenoon**

Time: 2 hours

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Part I - ten questions	10 X 4 = 40
Part II - fifteen questions	15 X 4 = 60
<b>Total</b>	<b>100</b>

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*Give your answers in the answer booklet only.*

*Write your Name, Registration Number, Test Centre, Test Code and the Number of this booklet in the appropriate places on the answer sheet.*

**STAPLE/ATTACH QUESTION BOOKLET WITH THE ANSWER BOOKLET. ALL ROUGH WORK MUST BE DONE ON THE QUESTION BOOKLET AND/OR ON THE ANSWER BOOKLET. YOU ARE NOT ALLOWED TO USE CALCULATOR.**

**WAIT FOR THE SIGNAL TO START WRITING**

## Part-I

(Ten questions, four marks each)

Select the right answer from the given alternatives for each of the following questions.

**10×4=40**

- For the ellipse  $5x^2 + 6y^2 = 15$ , the equations of a pair of conjugate diameters which are inclined to each other at an angle  $\tan^{-1} 11$  are
  - $x + y = 0$ ,  $5x - 6y = 0$  and  $x - y = 0$ ,  $5x + 6y = 0$
  - $x + y = 0$ ,  $6x - 5y = 0$  and  $x - y = 0$ ,  $6x + 5y = 0$
  - $x - y = 0$ ,  $7x - 8y = 0$  and  $x + y = 0$ ,  $8x + 7y = 0$
  - $x - y = 0$ ,  $8x - 7y = 0$  and  $x + y = 0$ ,  $7x + 8y = 0$
- The modulus of the expression  $\frac{3+4i}{12+5i}$  is
  - $\frac{5}{13}$
  - $\frac{6}{14}$
  - $\frac{7}{15}$
  - $\frac{9}{16}$
- If  $y = (\sin x)^{\log x}$ , the value of  $\frac{dy}{dx}$  is
  - $(\sin x)^{\log x} \left[ \frac{\log \sin x}{x} + \cot x \log x \right]$
  - $(\cos x)^{\frac{1}{x}} [\log \cos x + \sec x \log x]$
  - $(\tan x)^{\frac{1}{x}} [\log \tan x + \csc x \log x]$
  - $(\cot x)^{\log x} [\log \sec x + \tan x \log x]$
- The value of  $\lim_{x \rightarrow 0} \frac{\tan x - x}{x - \sin x}$  is
  - 2
  - 1
  - 0
  - 4

5. A function  $f(x)$  is defined in  $0 \leq x \leq 2$  by the equations

$$\begin{aligned} f(x) &= x & x < 1 \\ &= 1 + x & x > 1 \\ &= \frac{3}{2} & x = 1. \end{aligned}$$

The function  $f(x)$  is

- (a) continuous at  $x = 1$
- (b) discontinuous at  $x = 1$
- (c) differentiable at  $x = 1$
- (d) none of the above

6. The function  $f(x) = \sin^3 x \cos x$  has

- (a) a maximum at  $x = \frac{1}{3}\pi$
- (b) a minimum at  $x = \frac{1}{3}\pi$
- (c) neither a maximum nor a minimum
- (d) none of the above

7. The value of  $\lim_{n \rightarrow \infty} \left[ \left(1 + \frac{1}{n}\right) \left(1 + \frac{2}{n}\right) \dots \left(1 + \frac{n}{n}\right) \right]^{\frac{1}{n}}$  is

- (a)  $\frac{4}{e}$
- (b)  $\log 4 - 1$
- (c)  $\log 2$
- (d)  $\frac{1}{6}$

8. The value of  $\int \frac{\sin x}{\sin x + \cos x} dx$  is

- (a)  $\frac{1}{2}x - \frac{1}{2}\log(\sin x + \cos x)$
- (b)  $x - \log(\cos x - \sin x)$
- (c)  $\frac{1}{2}x + \frac{1}{2}\log(\tan x + \sec x)$
- (d)  $x + \log(\csc x + \cot x)$

9. If  $\omega$  is the cube root of unity, the value of the determinant

$$\begin{vmatrix} 1 & \omega & \omega^2 \\ \omega & \omega^2 & 1 \\ \omega^2 & 1 & \omega \end{vmatrix} \text{ is}$$

- (a) 0

- (b) 1
- (c) -1
- (d)  $\omega$

10. The eigenvalues and the corresponding eigenvectors of the matrix

$$\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$

are

- (a) 2,  $[-1 \ 0 \ 2]'$ ; 2,  $[1 \ 2 \ 0]'$ ; 8,  $[2 \ -1 \ 1]'$
- (b) 3,  $[1 \ 0 \ 3]'$ ; 3,  $[2 \ 3 \ 0]'$ ; 7,  $[1 \ -2 \ 1]'$
- (c) 15,  $[2 \ 1 \ -2]'$ ; 0,  $[2 \ 2 \ 1]'$ ; 3,  $[1 \ 2 \ 2]'$
- (d) none of the above

## Part-II

(Fifteen questions, four marks each)

11. The ridge push ( $F_{rp}$ ) and slab pull ( $F_{sp}$ ) are two dominant plate driving mechanisms. These two forces can be quantified as:

$$a) F_{rp} = g \rho_m \alpha_v (T_m - T_0) \left( 1 + \frac{2 \rho_m \alpha_v (T_m - T_0)}{\pi (\rho_m - \rho_0)} \right) \kappa t$$

$$F_{sp} = M_e g$$

$$b) F_{rp} = g \rho_m \alpha_v (T_m - T_0) \left( 1 + \frac{2 \rho_m \alpha_v (T_m - T_0)}{\pi (\rho_m - \rho_0)} \right)$$

$$F_{sp} = M_e g$$

$$c) F_{rp} = g \rho_m (T_m - T_0) \left( 1 + \frac{2 \rho_m (T_m - T_0)}{\pi (\rho_m - \rho_0)} \right) \kappa t$$

$$F_{sp} = M_e g$$

$$d) F_{rp} = \rho_m \alpha_v (T_m - T_0) \left( 1 + \frac{2\rho_m \alpha_v (T_m - T_0)}{\pi(\rho_m - \rho_0)} \right) \kappa t$$

$$F_{sp} = M_e g$$

$\alpha_v$ =thermal expansion coefficient;  $K$  = thermal diffusivity;  $M_e$  = excess mass

12. An iceberg has a density of  $950.0 \text{ kg m}^{-3}$ . What fraction of its volume is submerged in sea water having density of  $1025.0 \text{ kg m}^{-3}$ ? (Hint:  $\rho_1 g V_1 = \rho_2 g V_2$ )

- a) 92.7
- b) 90.1
- c) 93.0
- d) 91.5

13. A tracer is diffused from a region of high concentration ( $C_0$  at  $y = 0$ ) towards a region (at  $y = h$ ) where the concentration is kept very low (by constant replacement). Assume that the diffusion coefficient  $D$  is constant. Then the concentration profile will be (Hint: Fick's second law is  $d^2C/dy^2 = 0$ ):

- a)  $C = C_0(1-y/h)$
- b)  $C = C(y-y/h)$
- c)  $C = C_0(y-y/h^2)$
- d)  $C = C_0(h-y^2/h^2)$

14. A debris flow of 2.0 m thick moves down a slope inclined at an angle  $\alpha = 5.7$  degrees, equivalent to  $\sin \alpha = 0.1$ . The bulk density of the flow was found to be  $2400 \text{ kg m}^{-3}$ . The debris approximated a Bingham material with shear strength equal to  $4 \times 10^3 \text{ Pa}$ , and a viscosity of  $400 \text{ Pa s}$ . The thickness of the rigid plug will be: (Hint: shear stress varies linearly with distance from surface to the flow,  $Y$ ):

- a)  $Y = 1.7\text{m}$
- b)  $Y = 17.0\text{m}$
- c)  $Y = 0.17\text{m}$
- d)  $Y = 2.0\text{m}$

15. A vector  $\begin{pmatrix} x \\ y \end{pmatrix}$  is transformed to  $\begin{pmatrix} x' \\ y' \end{pmatrix}$  by a transformation which can be written as  $\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$ , where  $\begin{pmatrix} 1 & 1 \\ 0 & 1 \end{pmatrix}$  is the transformation matrix. If the original vector is given by  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ , the transformed vector and its orientation with respect to x-axis are given by

(a)  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ ,  $\sin^{-1}(1/\sqrt{3})$

(b)  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ ,  $\sin^{-1}(1/\sqrt{2})$

(c)  $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$ ,  $\sin^{-1}(1/\sqrt{5})$

(d)  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ ,  $\sin^{-1}(1/\sqrt{5})$ .

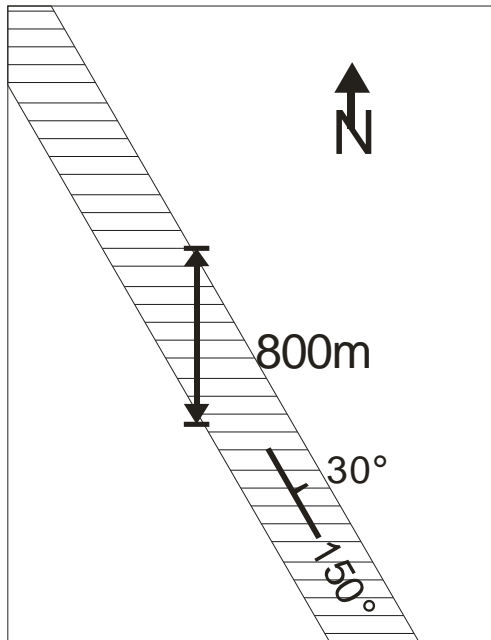
16. Slickensides on a fault plane dipping  $60^\circ$  toward East show a pitch of  $30^\circ$  N. A horizontal coal seam displaced by this oblique slip fault shows a vertical throw of 50 metres, with hanging wall going down relative to footwall. The correct amount of strike slip component in metres is given by

(a)  $100/3$

(b)  $100/\sqrt{3}$

(c)  $100\sqrt{3}$

(d)  $100/2$ .



17. The true thickness of the bed (shown by hatch symbol in sketch above) is:

- a) 200m
- b) 300m
- c) 800m
- d) 1600m

18. 500 chert pebbles measured on a beach have mean sphericity of 0.71, standard deviation is 0.08. How many pebbles are expected to have sphericity values greater than 0.79, assuming the distribution is normal?

- a) 92.
- b) 79.
- c) 40.
- d) 57.

19. A cladogram is based on the hierarchical progression of shared characters and the character states can be:

- a) Both numeric and descriptive (non numeric).
- b) Only numeric.

- c) 90% numeric.
- d) 95% numeric.

20. Length of five specimens of temnospondyl amphibians measured in mm are; 205, 255, 220, 195, 235. The 'Variance (s)' of the length data will be:

- a) 23.88.
- b) 1110.
- c) 570.
- d) 2280

21. If the fluid potential is given by  $\phi = x^2 + xy + yz$  then at the point (2, 1, 4) the coordinates of the unit vector pointing in the direction of maximum rate of change of the potential will be:

- a)  $\mathbf{r} = 0.635\mathbf{i} + 0.762\mathbf{j} + 0.127\mathbf{k}$
- b)  $\mathbf{r} = 0.65\mathbf{i} + 0.72\mathbf{j} + 0.17\mathbf{k}$
- c)  $\mathbf{r} = 0.0635\mathbf{i} + 0.0762\mathbf{j} + 0.0127\mathbf{k}$
- d)  $\mathbf{r} = 6.35\mathbf{i} + 7.62\mathbf{j} + 1.27\mathbf{k}$

22. In a volcanic eruption from a cone which rises 300 m above the surrounding (flat) countryside, large bombs are observed to be thrown a maximum distance of 3000 m. neglecting air resistance, and assuming that the initial angle of ejection was 45 degrees, the speed at which they will hit the ground will be:

- a)  $180.6 \text{ m s}^{-1}$
- b)  $18.06 \text{ m s}^{-1}$
- c)  $1.806 \text{ m s}^{-1}$
- d)  $0.1806 \text{ m s}^{-1}$

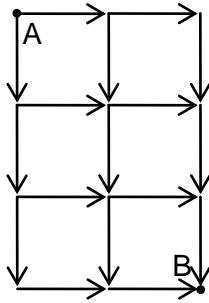
23. If the left and the right banks of a river could be represented by the following two equations, respectively:

$$y = 50 \sin(x) + 150 \text{ and } y = -30 \cos(x) + 60$$

Then the maximum width of the river along y is:

- a) 170
- b) 140
- c) 120
- d) 80





24. The channel segments in a braided river system are shown above. Water in the channels can move only in the directions indicated by the arrow heads (i.e., either to the east or to the south). If the total number of east-west segment is  $e$  and north-south segment is  $s$  then the number of total number of possible paths through which water can flow from A to B is:

- a)  $\frac{(e+s)!}{e!s!}$
- b)  $\frac{e!+s!}{e!s!}$
- c)  $e! + s!$
- d)  $e!s!$

25. If a one centimeter cube block of sediment is internally made up of perfectly spherical grains of 10mm diameter then the maximum porosity is:

- a) Less than 35%
- b) Less than 25%
- c) Greater than 45%
- d) Greater than 55%